

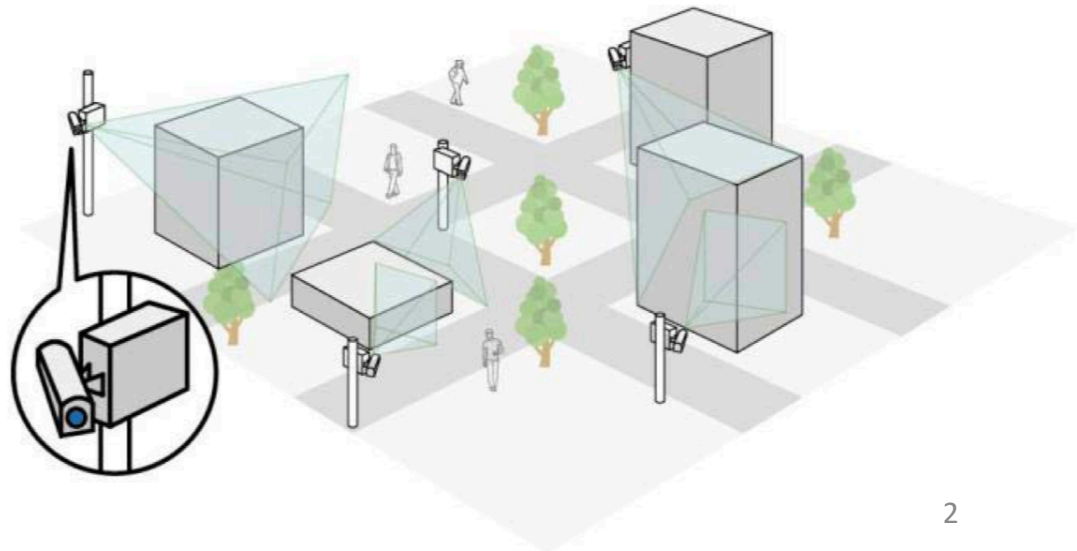
# Camera Placement in Smart Cities for Maximizing Weighted Coverage With Budget Limit

*IEEE SENSORS JOURNAL, VOL. 17, NO. 23, DECEMBER  
1, 2017*

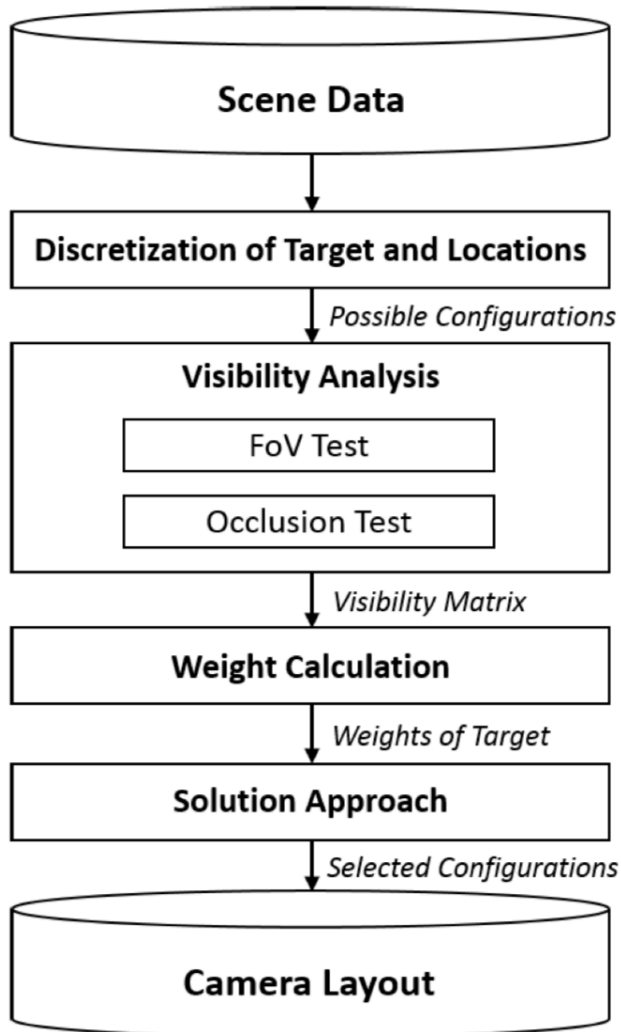
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Seokcheon Lee

# Introduction

- Video surveillance systems incorporating wireless camera networks have played significant roles in the management of core infrastructures.
- This paper address the camera placement problem for minimization of weighted coverage under a budget limitation in a 3D environment.
- They develop a heuristic algorithm.



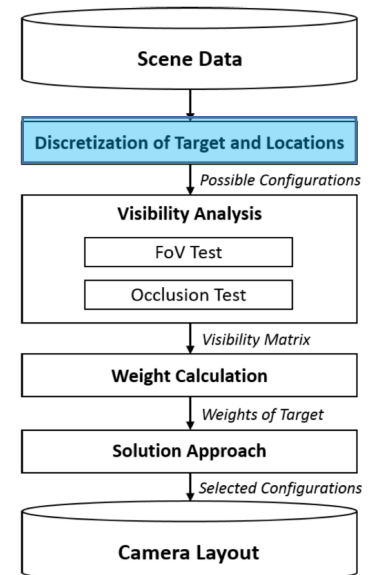
# Collaboration-based Local Search Algorithm (COLSA)



- Framework for solving camera placement problem

# Collaboration-based Local Search Algorithm (COLSA)

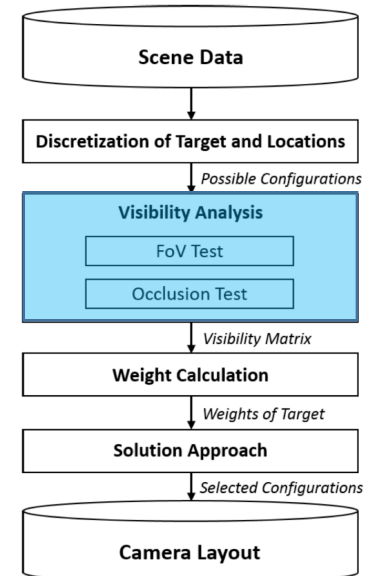
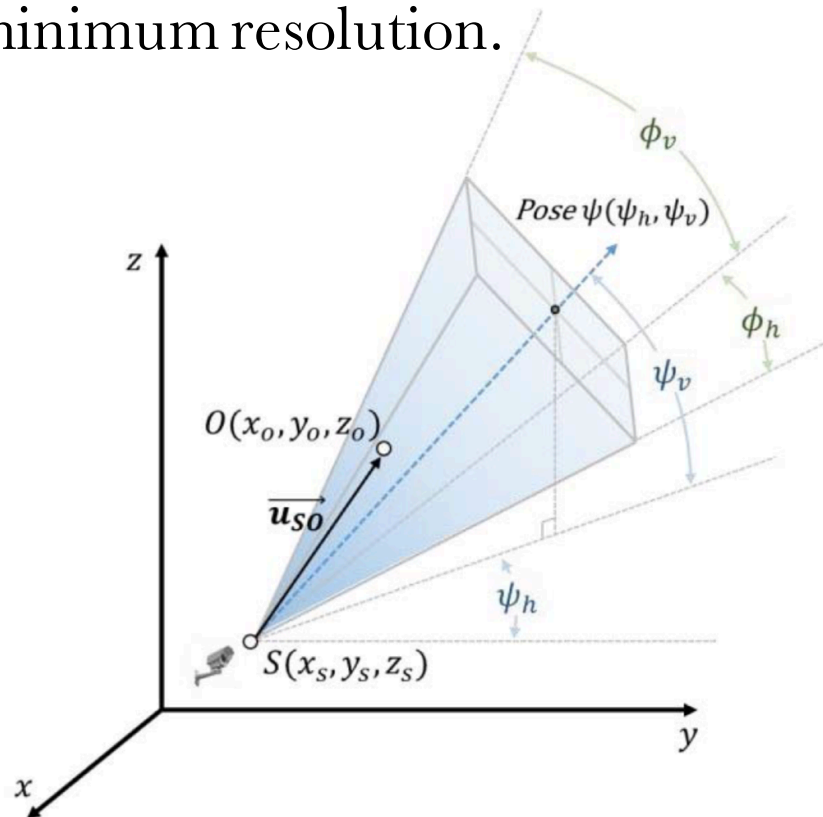
- Discretization of Target and Location
  - Discretization of the the target and camera locations into 3D grid points
  - To reduce the computation time of the entire methodology
  - The computation time of visibility analysis is inversely proportional to the grid size



# Collaboration-based Local Search Algorithm (COLSA)

- Field of View Test

- The FoV area calculate between working distance, horizontal and vertical viewing angle, and the pose.
- The working distance and the camera viewing angle can be required minimum resolution.



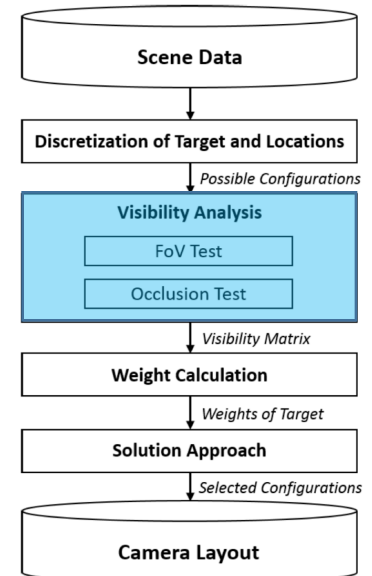
# Collaboration-based Local Search Algorithm (COLSA)

- Field of View Test

- Confirm whether a camera position  $s$  can cover a target point  $o$ . The constrain shows as follow:

$$\begin{aligned}\vec{u}_{so} &= \vec{o} - \vec{s} \\ \psi_h - \frac{\phi_h}{2} &\leq \arctan\left(\frac{x_o - x_s}{y_o - y_s}\right) \leq \psi_h + \frac{\phi_h}{2} \\ \psi_v - \frac{\phi_v}{2} &\leq \arcsin\left(\frac{z_o - z_s}{\|\vec{u}_{so}\|}\right) \leq \psi_v + \frac{\phi_v}{2} \\ \|\vec{u}_{so}\| &\leq d\end{aligned}$$

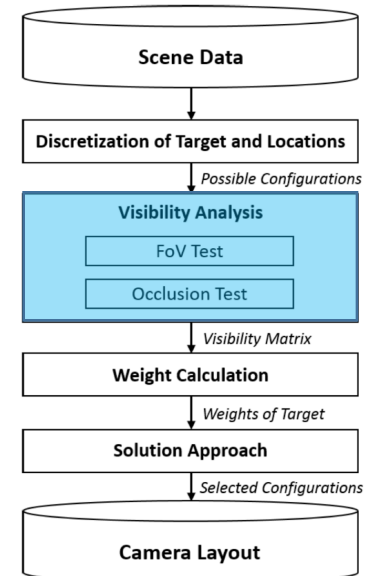
$o$ : target point,  $s$ : camera position,  $\psi$ : pose



# Collaboration-based Local Search Algorithm (COLSA)

- Field of View Test
  - Select three different types of camera and calculate the working distance.

Camera Types	A	B	C
Vertical Angle ( $\phi_v$ )	51.45	60.95	60.62
Horizontal Angle ( $\phi_h$ )	93.91	105.19	104.82
Working distance with zooming ( $d$ ) (meters)	27.5	15	11.3
Price (USD)	1085	429	379



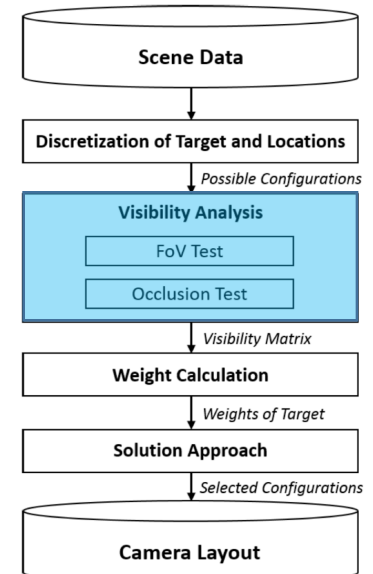
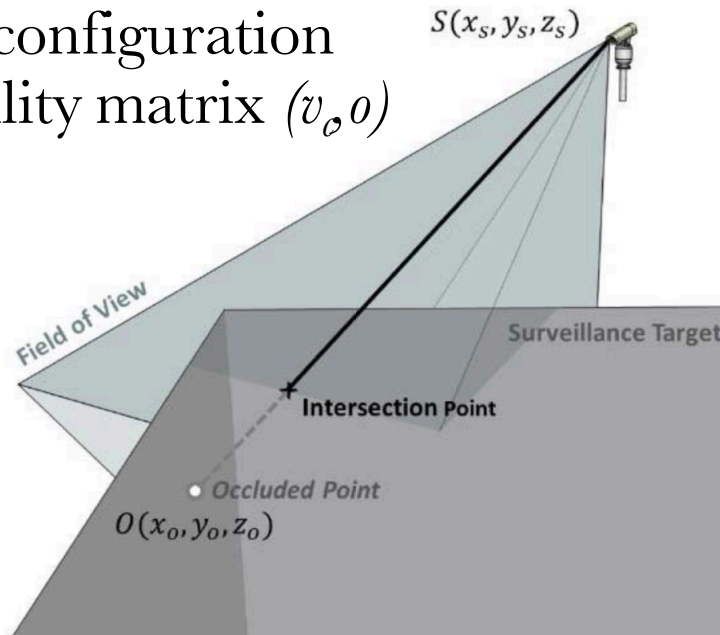
# Collaboration-based Local Search Algorithm (COLSA)

- Occlusion Test

- The gray dotted line in the following figure represents the invisible area occluded by the plane of a surveillance target itself.

- Visibility Analysis

- A Candidate Camera Configuration: position, camera type, azimuth, elevation
- Candidate camera configuration is saved in the visibility matrix  $(v_{\phi, \theta})$



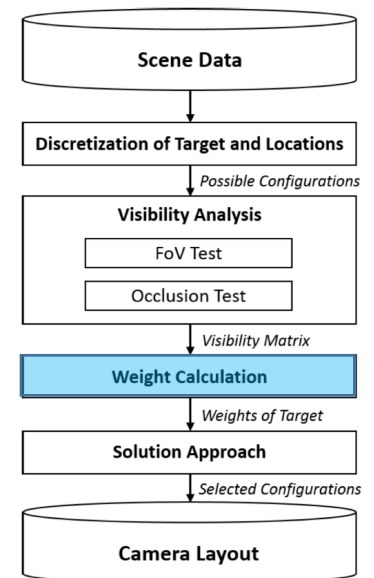
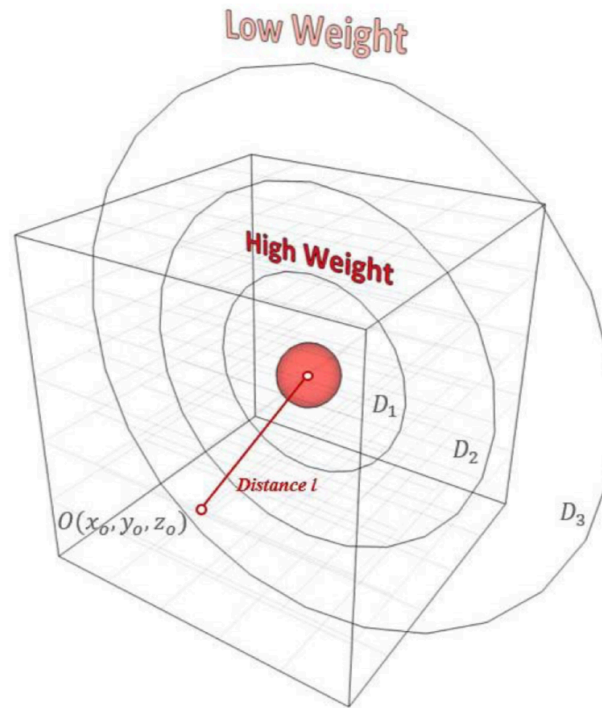


# Collaboration-based Local Search Algorithm (COLSA)

$$w_o = \begin{cases} 3 & (\text{if } l < D_1) \\ 2 & (\text{if } D_1 \leq l < D_2) \\ 1 & (\text{if } D_2 \leq l) \end{cases}$$

$$R(\%) = \frac{\sum_{o \in O} w_o \times y_o}{\sum_{o \in O} w_o} \times 100$$

R: weighted coverage rate,  
 $y_0 = 1$ , the target point is coverage  
 $y_0 = 0$ , the target point is not coverage



# Collaboration-based Local Search Algorithm (COLSA)

- Mathematical Representation

$$\begin{aligned}
 & \text{maximize} \quad \sum_{o \in O} w_o \cdot y_o / \sum_{o \in O} w_o \\
 & \text{subject to} \quad \sum_{(s, j_s) \in V_o} c_s \cdot x_{s, j_s} \leq B \\
 & \quad \quad \quad \sum_{(s, j_s) \in V_o} x_{s, j_s} \geq y_o \\
 & \quad \quad \quad \sum_{j_s} x_{s, j_s} = 1 \quad \forall s \in S \\
 & \quad \quad \quad x_{s, j_s} \in \{0, 1\} \quad \forall s \in S \\
 & \quad \quad \quad y_o \in \{0, 1\} \quad \forall o \in O
 \end{aligned}$$

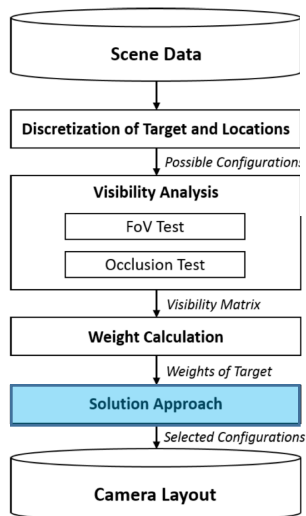
Indices	$s$	Index of cameras, $s \in S$
	$o$	Index of target points, $o \in O$
	$j_s$	Index of configurations of camera $s$
Parameters	$w_o$	Weight of target points
	$c_s$	Cost of cameras
	$B$	Budget Limitation
Set	$V_o$	Cameras and their configurations that cover target point $o$
Decision Variables	$y_o$	If a target point $o$ is covered by the selected camera configurations, $y_o = 1$ ; otherwise, $y_o = 0$ .
	$x_{s, j_s}$	If a configuration $j_s$ is chosen for camera $s$ , $x_{s, j_s} = 1$ ; otherwise, $x_{s, j_s} = 0$ .

# Collaboration-based Local Search Algorithm (COLSA)

1. Calculate the  $c_o$
2. Calculate the  $cr_s$
3. Select the  $c'$  with highest  $cr_s$  until reach the budget limit

$$c_o = \frac{n_c - \sum_{c \in C} v_{c,o}}{n_c} \times \prod_{c \in C'} (1 - v_{c,o})$$

$$cr_c = \frac{\sum_{o \in O} (w_o \cdot c_o)}{K_c}$$




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## Algorithm 1 Collaborative Allocation Phase

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**input** :  $C = \{\text{set of camera configurations}\}$ ;  $O = \{\text{set of targets}\}$ ;  $v_{c,o} = \{\text{visibility matrix}\}$

**output** :  $C' = \text{Chosen Camera Configurations}$

Set  $C' = \emptyset$

Set  $TC = 0$ .

**While**  $(\sum_c cr_c \neq 0$  or  $C \neq \emptyset$  or  $O \neq \emptyset$  or  $TC = 0)$  **do**

**for** (camera configuration  $c \in \{1, 2, \dots, C\}$ ) **do**

**for** (target point  $o \in O$ ) **do**

Compute the relative chance  $c_o$  to be covered using (13)  $\forall o \in \{1, 2, \dots, O\}$ .

**End for**

Update  $cr_c \forall c \in C$  according to (14).

Select  $c'$  with the highest  $cr_c$ .

**If**  $(\sum_c K_c + K_{s'} \geq B)$  **then**

Set  $TC = 1$ .

**Exit for**

**else**

Set  $c'$  in  $C'$ .

**End if**

Remove target points covered by  $c'$  from  $O$ .

Remove  $c'$  from  $C$ .

**End for**

**end while**

Return  $C$ .

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# Collaboration-based Local Search Algorithm (COLSA)

1. Adjust the sensing orientations
2. Calculate the weighted coverage rate

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## Algorithm 2 Local Search Phase

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**input** :  $C'$  = Chosen Camera Configurations of Algorithm 1;  
 $DX$ ;  $DY$ ;  $DZ$ ;  $DH$ ;  $DV$

**output** :  $C''$  = Improved Camera Configurations by local search phase

Set  $DX, DY, DZ = \{-1, 0, 1\}$ .

Set  $DH = \{-30, -15, 0, 15, 30\}$ .

Set  $DV = \{-40, -20, 0, 20, 40\}$ .

$C'' \leftarrow C'$ .

**For** (camera configuration  $c \in C''$ ) **do**

Set  $N = \emptyset$

Initialize  $c'$

**for** (each  $d_x \in DX, d_y \in DY, d_z \in DZ, d_h \in DH$ , and  $d_v \in DV$ ) **do**

Set  $x_{c'}$  to  $x_c + d_x$

Set  $y_{c'}$  to  $y_c + d_y$

Set  $z_{c'}$  to  $z_c + d_z$

Set  $\psi_h$  of  $c'$  to  $\psi_h + d_h$

Set  $\psi_v$  of  $c'$  to  $\psi_v + d_v$

Initialize  $C_n$

$C_n \leftarrow C'$ .

Change  $c \in C_n$  to  $c'$ .

Add  $C_n$  to  $N$ .

**end for**

**end for**

**for** (camera configuration  $C_n \in N$ ) **do**

Calculate the weighted coverage rate of  $C_n$  using (5)

**end for**

find the best  $C_{nb}$  in  $N$ .

**if** (there is no improvement between  $C_{nb}$  and  $C''$ ) **then**

**exit for**

**else**

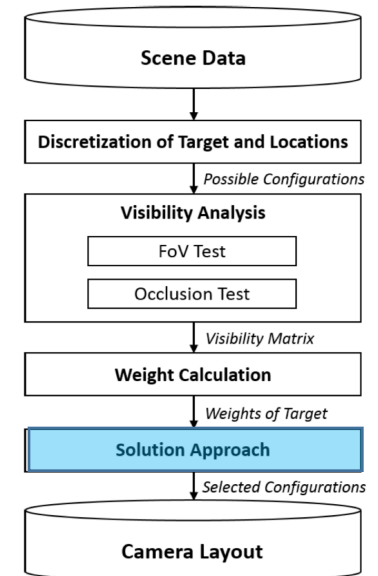
$C'' \leftarrow C_{nb}$ .

**end if**

**end for**

Return  $C''$

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# Experiment

- Experiment Design

Parameters	Small Size	Large size
Maximum size of 3D space ( $x_s, y_s, z_s$ ) (meter)	(500, 500, 500)	
Azimuth ( $\psi_h$ )	0°, 45°, 90°, 135°, 180°, 225°, 270°, 315°	
Elevation ( $\psi_v$ )	30°, 330°, 150°, 210°, 270°	
Average number of camera configurations	42309	73673
Average number of target points	4112	12820
Average total weights	8658	28069
Length of target for each edge (meter)	N(30, 5)	N(50, 10)
Distance between target grid points ( $\Delta_o$ ) (meter)	1	1
Distance between camera grid points ( $\Delta_s$ ) (meter)	4	6
Minimum covered target points	10	20
Average computation time for visibility analysis (minutes)	11.63	26.76

# Experiment

- Experiment Result
  - Non-weighted

Budget Limitation (USD)	Algorithms	Small		Large	
		Computation Time (Min)	Coverage Rate (%)	Computation Time (Min)	Coverage Rate (%)
5,000	BPSO	1.72	28.55	14.44	11.22
	BGA	2.71	40.88	22.51	19.59
	Greedy	0.16	48.03	0.7	20.07
	COLSA	0.54	52.75	1.92	20.94
10,000	BPSO	1.9	40.8	16.3	18.21
	BGA	2.72	61.83	23.35	33.02
	Greedy	0.31	71.17	1.54	37.98
	COLSA	1.17	81.24	3.56	41
20,000	BPSO	19.73	60.35	53.51	29.72
	BGA	9.44	79.7	41.47	48.44
	Greedy	0.61	96.3	2.96	62.37
	COLSA	2.1	98.5	5.98	66.65

# Experiment

- Experiment Result

- Weighted

Budget Limitation (USD)	Algorithms	Small		Large	
		Computation Time (Min)	Weighted Coverage Rate (%)	Computation Time (Min)	Weighted Coverage Rate (%)
5,000	BPSO	2.21	25.97	18.05	11.26
	BGA	2.71	41.44	22.48	20.34
	Greedy	0.21	46.1	0.85	19.1
	COLSA	0.68	52.08	2.56	22.24
10,000	BPSO	2.4	38.76	19.15	17
	BGA	2.77	60.43	23.05	33.94
	Greedy	0.4	73.74	1.83	37.67
	COLSA	1.3	80.3	4.62	40.62
20,000	BPSO	19.87	55.81	42.81	27.32
	BGA	9.51	78.3	34.4	49.18
	Greedy	0.79	96.02	3.63	61.92
	COLSA	2.54	98.39	8.35	66.85

# Conclusion

- Addressing of the camera placement problem for maximized weighted coverage with the budget limitation in a 3D environment
- Developing of a new heuristic algorithm
- The second phase of proposed algorithm can be applied extensively for adjustment of angles



Questions?

# Literature Review

- Much work relating to camera placement problems for maximization of surveillance target.
- The camera placement problems for maximization of surveillance problem under budget limitations in 3D environment has been far less study.

