

Matlab 4: Matrix



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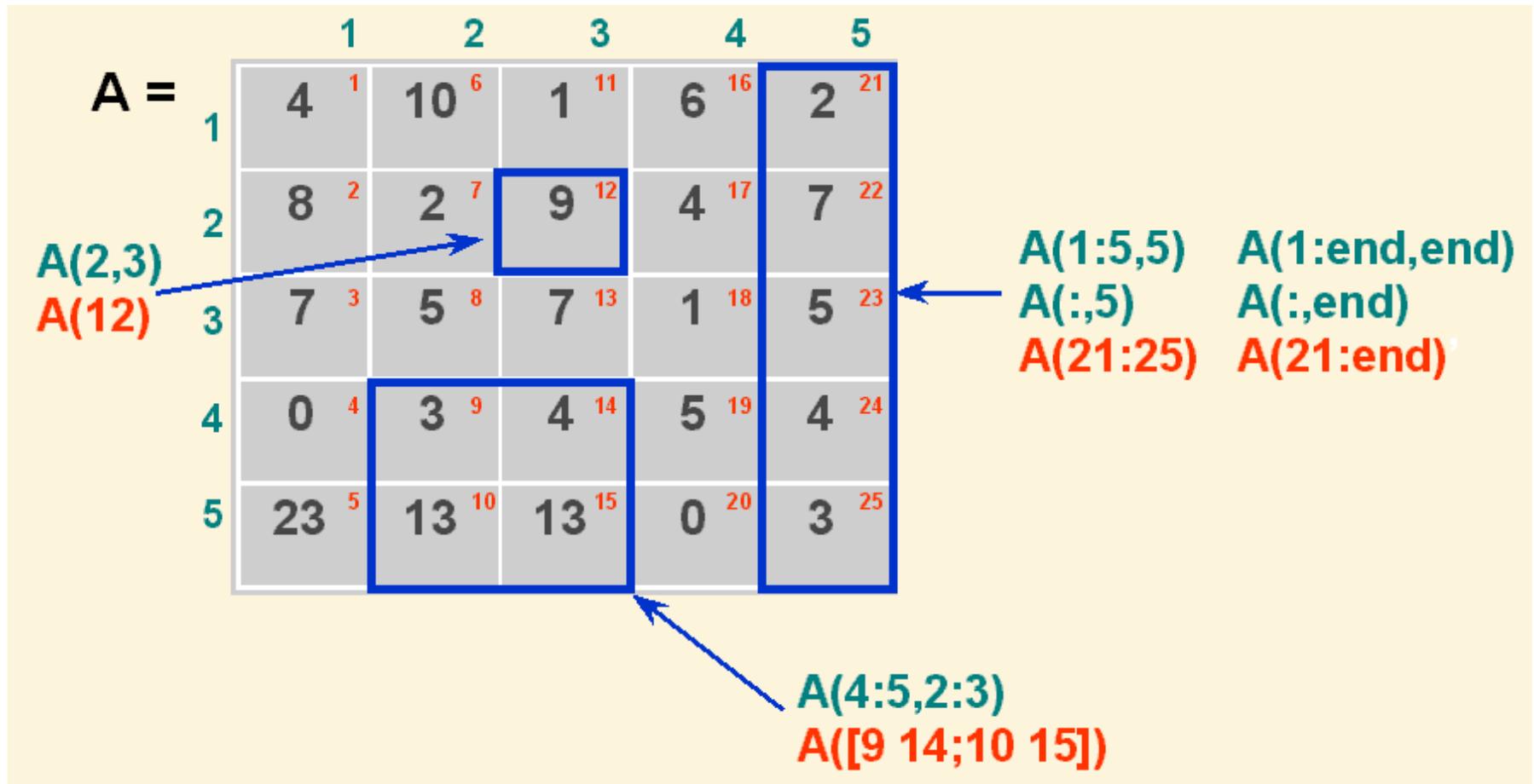
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Slides are based on the materials from Prof. Roger Jang

Matrix Indexes and Subscripts

- In Matlab, $A(i, j)$ denotes the i -th row, j -th column element of matrix A
 - i and j are the indexes or subscripts of the element
- Matlab adopts column-wise indexes
 - We can use 1- or 2-dimensional indexes to access the same elements
 - $A(i, j)$ and $A(i+(j-1)*m)$ are the same, where m is the number of rows

1- and 2-dimensional Indexes



Indexing Part of A Matrix

- $A(4:5,2:3)$ refers to rows 4 and 5, columns 2 and 3
 - $A([9\ 14; 10\ 15])$ points to the same 2x2 sub-matrix
- $:$ indicates the whole row or column
 - $A(:,5)$ refers to the 5th column of A
- end indicates the last element of a dimension
 - $A(:,\text{end})$ is the last (right-most) column of A
- Use $[]$ to delete a column or row
 - $A(2, :) = [] \leftarrow$ remove the row 2 completely

More Matrix Manipulations

- Create a bigger matrix
 - $A = \text{magic}(5)$
 - $B = [A \ 1./A]$
 - $C = [B; 1./B]$
- Retrieve elements along the diagonal
 - $D = \text{diag}(A)$
- Generate a diagonal matrix
 - $E = \text{diag}([1, 2, 3, 4])$

More Matrix Manipulations (cont.)

- Multiply column/row vectors
 - $V = [1; 2; 3; 4; 5]; B = \text{magic}(5);$
 - $B * B$
 - $V' * B$
- Reshape flattens a matrix into a column vector and then put individual elements into an $m \times n$ matrix
 - $A = \text{magic}(4)$
 - $B = \text{reshape}(A, 2, 8)$

Matrix Generation Functions

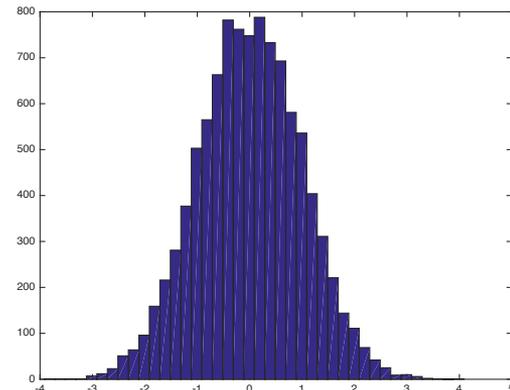
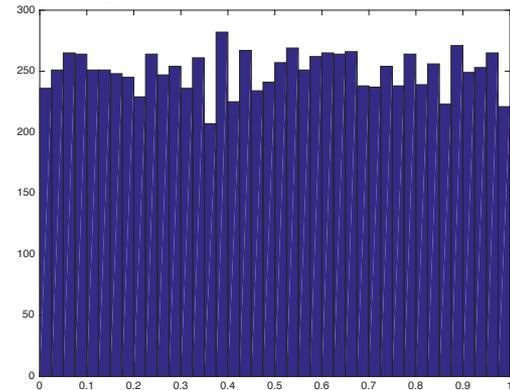
- `zeros(m, n)`: all elements are 0
- `ones(m, n)`: all elements are 1
- `eye(n)`: identity matrix
- `pascal(n)`: Pascal matrix
- `vander(v)`: Vandermonde matrix, columns are powers of v
- `rand(m, n)`: $m \times n$ random matrix, uniform distribution
- `randn(m, n)`: $m \times n$ random matrix, zero mean, unit variance Gaussian distribution
- `hilb(n)`: $n \times n$ Hilbert matrix \leftarrow ill-conditioned matrix
- `magic(n)`: $n \times n$ matrix with equal sums among rows, columns, and diagonals

Hilbert Matrix

- Hilbert matrix is defined as $H_{ij} = \frac{1}{i+j-1}$
 - Larger Hilbert matrices are closer to singular (not invertible, determinant is zero)
 - Observe: `hilb(3)`, `inv(hilb(3))`, `hilb(12)`, `inv(hilb(12))`
 - Given $Ax = b$, matrix A is **ill-conditioned** if a small changes on b 's values leads to large changes on vector x ← **challenging matrices to algorithms**

Uniform and Gaussian Distributions

- rand: random numbers following uniform distribution
 - `x1 = rand(10000, 1);`
 - `hist(x1, 40)`
- randn: Gaussian distribution
 - `x1 = randn(10000, 1);`
 - `hist(x1, 40)`



Matrix Addition and Subtraction

- Matrix addition/subtraction are done between matrices with the same size
 - $\gg [1, 2, 3] + [4, 5, 6]$
 - ans = 5 7 9
- Addition/subtraction between a matrix and a scalar \rightarrow the scalar is applied to all elements
 - $\gg 10 + [4, 5, 6]$
 - ans = 14 15 16

Matrix Multiplication/Division

- Scalar multiplication/division
 - $[1, 2, 3] * 12$
 - $[1, 2, 3] / 2$
- Multiplication of two matrices: the column number of the 1st matrix must be the same as the row number of the 2nd matrix
 - $A = [1; 2];$
 - $B = [3, 4, 5];$
 - $C = A * B$
- Division of two matrices: using inverse matrix or solving equation systems

Power and Element-by-Element Operations

- Matrix power: meaningful for squares
 - `magic(5) ^ 2` ← what does this do?
- Adding a `.` before `+`, `-`, `*`, `/` indicates element-by-element operations

```
A = [12; 45];
```

```
B = [2; 3];
```

```
C = A.*B
```

```
D = A./B
```

```
E = A.^2
```

Conjugate Transpose

- Conjugate transpose

- $z = [1+i, 2; 3, 1+2i];$

- $w = z'$

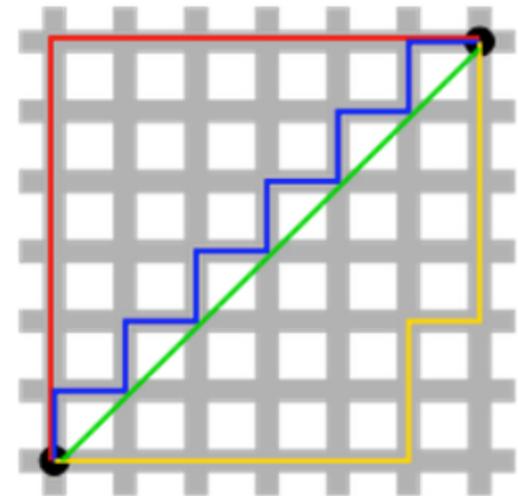
- Transpose

- $w = z.'$

- For real numbers, the conjugate transpose is the same as transpose

Vector's L_p -norm

- Vector a 's L_p norm is defined as $\|a\|_p = \left(\sum_i |a_i|^p \right)^{1/p}, p \geq 1$
 - $p=1 \rightarrow$ taxicab distance, or Manhattan distance
 - $p=2 \rightarrow$ Euclidean Length (length of a)
 - $p=\infty \rightarrow$ maximum distance
- $\text{norm}(x, p)$
 - $a = [3 \ 4];$
 - $\text{norm}(a, 1)$
 - $\text{norm}(a, 2)$
 - $\text{norm}(a, \infty)$



Exercise

- Prove

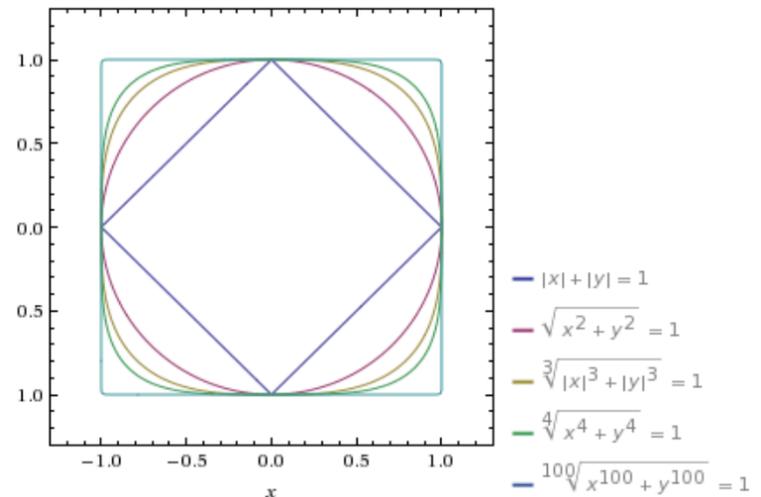
$$\|a\|_{\infty} \leq \|a\|_2 \leq \|a\|_1$$

- On a 2D space, plot the trajectory of

$$\|a\|_1 = 1$$

$$\|a\|_2 = 1$$

$$\|a\|_{\infty} = 1$$



Matrix's L_p -norm

- Matrix A 's L_p -norm is defined as $\|A\|_p = \max_x \frac{\|Ax\|_p}{\|x\|_p}$,
where $x \in R^n$
- `norm(...)` can be used for matrices as well
 - $A = [1\ 2\ 3; 4\ 5\ 6; 7\ 8\ 9];$
 - `norm(A, 2)`

Sorting a Vector

- Sort the elements in a vector
 - $x = [3 \ 5 \ 8 \ 1 \ 4];$
 - $[\text{sorted}, \text{index}] = \text{sort}(x)$
- Sorted is the new vector, index is the position of the sorted elements in the original vector
 - Hence, $x(\text{index})$ is equivalent to the sorted vector
- Exercise: how to get vector x using sorted and index
 - $[\sim, \text{rindex}] = \text{sort}(\text{index})$
 - $\text{sorted}(\text{rindex})$

Locating the Maximum in Each Column

- `>> x = magic(5);`
`[colMax, colMaxIndex] = max(x)`
`colMax = 23 24 25 21 22`
`colMaxIndex = 2 1 5 4 3`
- `>> [maxValue, maxIndex] = max(colMax);`
- `>> fprintf('Max value = x(%d, %d) = %d\n',`
`colMaxIndex(maxIndex), maxIndex, maxValue);`
`Max value = x(5, 3) = 25`
- Just to find the max value: `max(max(x))` or `max(x(:))`

Array Element Data Types

- Double by default, but recent versions support additional data types

Data Type	Description
uint8	Unsigned 8-bit integer, range: [0,255]
uint16	Unsigned 16-bit integer, range: [0,65535]
uint32	Unsigned 32-bit integer, range: [0,2 ³² -1]
int8	Signed 8-bit integer, range: [-128,127]
int16	Signed 16-bit integer, range: [-32768,32767]
int32	Signed 32-bit integer, range: [-2 ³¹ ,2 ³¹ -1]
single	32-bit single precision floating number
double	64-bit double precision floating number
char	16-bit character

Memory Usage of Different Data Types

- `x_double = magic(10);`
- `x_single = single(x_double);` ← **casting**
- `x32 = uint32(x_double);`
- `x16 = uint16(x_double);`
- `x8 = uint8(x_double);`
- `whos` ← **show the memory consumption**
- Sample observation: `uint8` array consumes 1/8 of memory compared to `double`

Tips on Choosing Data Types

- Out of range integers
 - `uint8(999)`
 - `uint8(-999)`
- Variables in different data types can be compared (after implicit conversions)
 - `uint8(20)== 20` ← `try uint8(-10)...`
- Explicit conversions may be necessary
 - `z=uint8(2.54) * 2.5`
 - `z * 3.33`
 - `double(z) * 3.33`

Strings and Characters

- A string consists of a sequence of characters
- In Matlab, a string can be seen as a row vector of characters, encoded in ASCII
- Matlab uses single quotation marks for string boundary; two strings can be concatenated
 - `str1 = 'Taipei zoo displays animals from Taiwan';`
`str2 = ', Australia, Africa, and desert.'; [str1 str2]`
- If you get lost: **help strfun**

Escape Character and Length

- For a string with single quote, add an extra single quote
 - 'I've got homework to do. '
- Use length to calculate the number of characters in a string
 - `length('I've got homework to do.')`

Conversions between ASCII and String

- double: convert human-readable string into ASCII vector
- char: convert ASCII vector into human-readable string
 - `s = 'I've got homework to do.';`
 - `a_asc = double(s)`
 - `s2 = char (a_asc)`

Storage Usage of Characters

- `>> whos s2`

Name	Size	Bytes	Class
Attributes			
s2	1x24	48	char

- Each character consumes 2 bytes, even for ASCII
 - Internally Matlab uses unicode, support CJK characters
- Can perform operations on string as if it's a double vector
 - `double(s2)`
 - `s2 + 1`

Execute Dynamically-Composed Commands

- Use `eval` to execute a string as if typing the command in the command window

```
for i = 2:5
    command = (['x', int2str(i) , '= magic('
, int2str(i) , ') '])
    eval(command);
end
```

Determine if a Variable is Char

- Two possibilities: class or ischar

```
>> class(s2)
```

```
ans =char
```

```
>> ischar(s2)
```

```
ans = 1
```

```
>> ischar(s2+1)
```

```
ans = 0
```

Storing Multiple Strings

- Save them as a two dimensional array
- But all strings should have the same length
 - departments = ['ee ', 'cs ', 'econ']
 - whos departments
- Or use char command
 - departments2 = char('ee', 'cs', 'econ')
 - whos departments2

Storing Multiple Strings (cont.)

- How to remove the extra trailing spaces?
 - deblank
- We will discuss a better solution (cell arrays) soon

```
>> departments(1, :)
```

```
ans = ee
```

```
>> length(departments(1, :))
```

```
ans = 4
```

```
>> length(deblank(departments(1, :)))
```

```
ans = 2
```

String Comparisons

- Matlab supports `strcmp`, which returns 1 if two strings are equivalent
 - Note that this is the opposite of C's `strcmp`
- `>> strcmp('elephant', 'bear')`
- `ans = 0`
- `>> strcmp('monkey', 'monkey')`
- `ans = 1`

Other String Related Commands

- `strcmpi`: ignore upper/lowercase
- `strncmp`: first n chars
- `findstr`: find a substring and return the index
- `strrep`: replace substrings

```
>> strrep('This is a monkey', 'monkey', 'bear')  
ans = This is a bear
```

Parsing Strings

- `strtok`: based on a delimiter (space by default), get the first token
- `strvcat`: merge multiple string into a 2-D array with automatic padding

```
input_string = 'ee cs econ stat me';
remainder = input_string;
parsed = '';
while (any(remainder))
    [chopped, remainder] = strtok(remainder);
    parsed = strvcat(parsed, chopped);
end
parsed
```

Conversion among Data Types

- `int2str`: convert integer into string
- `num2str`: convert real number into string
- `dec2hex`: convert decimal into hexadecimal
- `hex2num`, `hex2dec`, `bin2dec`, and others

Conversion between Strings and Arrays

- `mat2str`: convert matrix into string
- `eval`: convert string back to matrix

```
A = [1 2 1; 3 5 6 ];
```

```
B = mat2str(A)
```

```
A2 = eval(B)
```

```
isequal(A, A2)
```

Sprintf and Sscanf

- `>>str='pi'; newString = sprintf('%s is %d', str, pi)`
`newString = pi is 3.141593e+00`
- `>> str = '2 4.7 5.2';`
`mat = sscanf(str, '%f')`
`mat =`
2.0000
4.7000
5.2000
- `%s` indicates string, `%d` represents number,

Cell Array and How to Initialize It

- Store variables with different data types in the same array
- Approach #1: use { ... } on the right

```
A(1,1) = {'This is the first cell.'};
```

```
A(1,2) = {[5+j*6 , 4+j*5]};
```

```
A(2,1) = {[1 2 3; 4 5 6; 7 8 9]};
```

```
A(2,2) = {{'Tim'; 'Chris'}}
```

Resulting Cell Array

- The resulting 2x2 cell array

A(1,1) : 'This is the first cell.' String	A(1,2) : [5+j*6 4+j*5] 1x2 complex number array
A(2,1) : 1 2 3 4 5 6 7 8 9 3x3 integer array	A(2,2) : {'Tim', 'Chris'} 2x1 cell array

Initializing Cell Array

- In contrast to arrays, whereas we use (...) for indexing; for cell arrays, we use {...}
- Approach #2: use { ... } on the left (indexing)
 - `A{1,1} = 'this is the first cell.';`
 - `A{1,2} = [5+j*6, 4+j*5];`
 - `A{2,1} = [1 2 3; 4 5 6; 7 8 9];`
 - `A{2,2} = {'Tim'; 'Chris'}`

Initializing Cell Array (cont.)

- Approach #3: putting all elements in a single {...} (on the right)

```
>> B={'James Bond', [1 2;3 4;5 6]; pi, magic(5)}
```

```
>> C={rand(3), ones(2); zeros(5), randperm(4)}
```

Merging Two Cell Arrays

- Similar to merging two arrays

```
>> M = [B C]
```

```
M =
```

```
    'James Bond'    [3x2 double]    [3x3  
double]    [2x2 double]  
    [    3.1416]    [5x5 double]    [5x5  
double]    [1x4 double]
```

Showing the Content of Cell Array

- Directly printing a cell array only shows dimensions and data types
- Print an element in a cell array instead

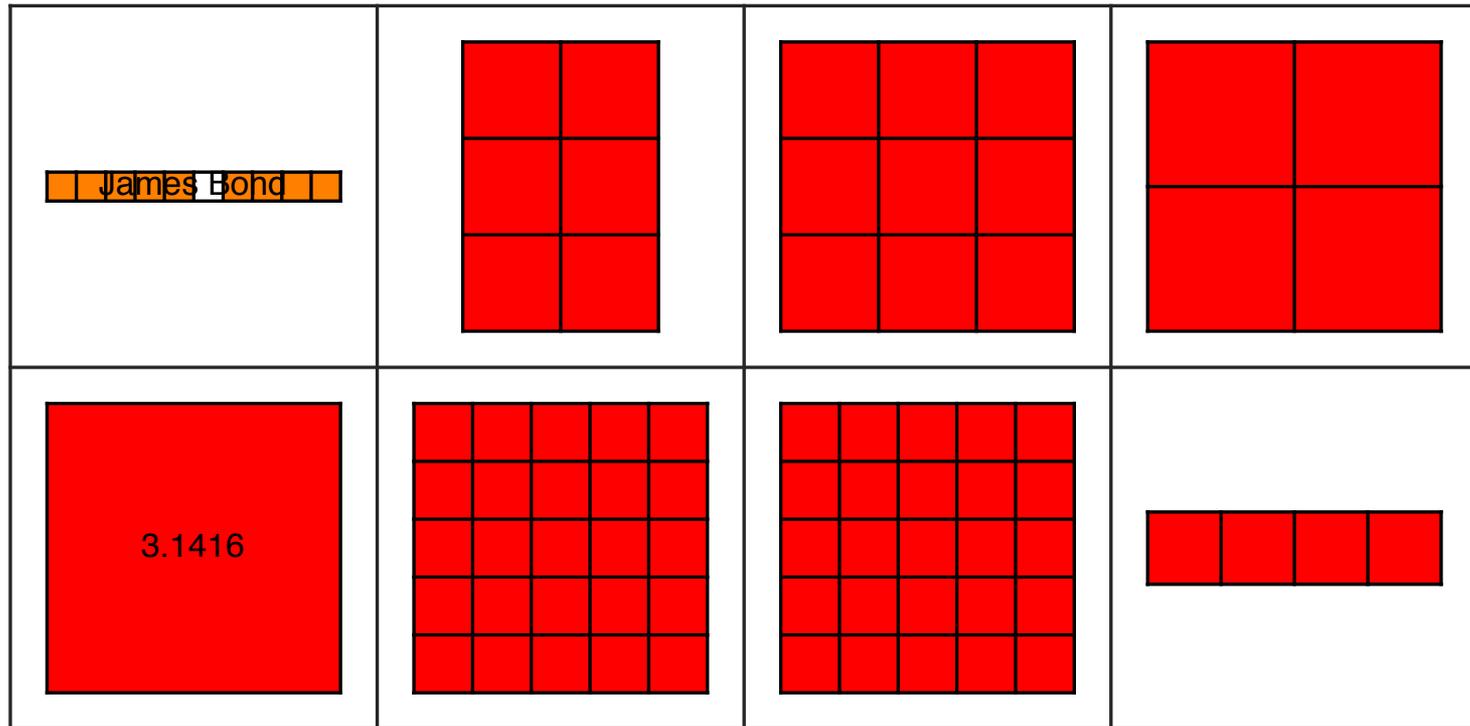
```
>> M
M = 'James Bond'      [3x2 double]      [3x3 double]      [2x2 double]
     [ 3.1416]        [5x5 double]      [5x5 double]      [1x4 double]
```

```
>> M{1,2}
ans =
     1     2
     3     4
     5     6
```

- Challenge: print all elements in a command?

Visualization of A Cell Array

- Cellplot(M): visualize cell array M



Display A Cell Array

- `celldisp(M)`: print cell array M

```
>> celldisp(M)
```

```
M{1,1} = James Bond
```

```
M{2,1} = 3.1416
```

```
M{1,2} =
```

```
    1    2
```

```
    3    4
```

```
    5    6
```

```
.....
```

Access Elements in Cell Arrays

- Get an element from a cell array

```
>> M{1,2}
```

```
ans =
```

```
    1    2  
    3    4  
    5    6
```

Access Elements in Cell Arrays (cont.)

- Get an element from an array within a cell array

```
>> M{1,2}(2,1)
```

```
ans = 3
```

Access/Remove Multiple Elements

```
>> size(M)
```

```
ans = 2      4
```

```
>> M(1,:)
```

```
ans = 'James Bond'      [3x2 double]      [3x3  
double]      [2x2 double]
```

```
>> M(1,:) = []
```

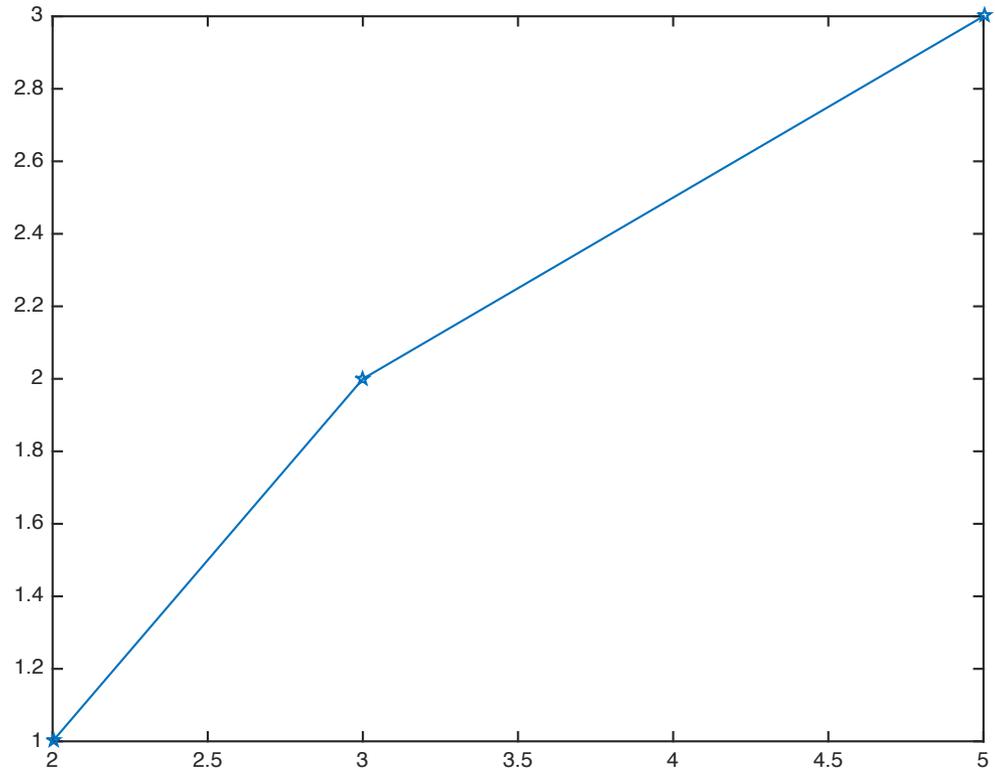
```
M = [3.1416]      [5x5 double]      [5x5 double]  
[1x4 double]
```

```
>> size(M)
```

```
ans = 1      4
```

Cell Arrays for Comma-Separated Arguments

- `F = {[2 3 5], [1 2 3], 'Timmy', 'Annie'};`
- `>> F{1:2}`
`ans = 2 3 5`
`ans = 1 2 3`
- `plot(F{1:2}, '-p')`



Comma-Separated Returns

```
>> [Z{1:2}] = max(rand(5))
```

```
Z = [1x5 double]      [1x5 double]
```

```
>> Z{1,1}
```

```
ans = 0.9294      0.8176      0.8116      0.9390      0.8443
```

```
>> Z{1,2}
```

```
ans = 1          4          3          1          5
```

Resize Cell Arrays

- Use (:

```
>> M
```

```
M =
```

```
    'James Bond'    [3x2 double]    [3x3 double]    [2x2 double]
    [    3.1416]    [5x5 double]    [5x5 double]    [1x4 double]
```

```
>> M(:)
```

```
ans =
```

```
    'James Bond'
    [    3.1416]
    [3x2 double]
    [5x5 double]
    [3x3 double]
    [5x5 double]
    [2x2 double]
    [1x4 double]
```

Resize Cell Arrays (cont.)

- Use reshape

```
>> B
```

```
B = 'James Bond'      [3x2 double]
```

```
    [ 3.1416]      [5x5 double]
```

```
>> N = reshape(B,1,4)
```

```
N = 'James Bond'      [3.1416]      [3x2 double]      [5x5  
double]
```

Pre-allocate and Test Cell Array

- `A = cell(4,3);` ← create a 4x3 empty cell array
- `iscell(A)` ← test if A is a cell array

```
>> A=cell(4,3)
```

```
A =
```

```
    []    []    []  
    []    []    []  
    []    []    []  
    []    []    []
```

```
>> iscell(A)
```

```
ans = 1
```

Convert Number Array to Cell Array

- $C = \text{num2cell}(A, \text{dim})$ \leftarrow convert a number array A into a cell array C , where dim is the dimension
- Default: each number becomes an 1x1 matrix in the cell array

```
>> A=[1, 2, 3; 4, 5, 6];
```

```
>> C=num2cell(A)
```

```
C = [1] [2] [3]
     [4] [5] [6]
```

Convert Number Array to Cell Array (cont.)

```
>> C=num2cell(A,1)
```

```
C = [2x1 double] [2x1 double] [2x1 double]
```

```
>> C=num2cell(A,2)
```

```
C = [1x3 double]  
     [1x3 double]
```

Convert Number Array to Cell Array (cont.)

- Exercise: `mat2cell(.)` supports more sophisticated conversions

```
>> X = [1 2 3 4; 5 6 7 8; 9 10 11 12]
C = mat2cell(X, [1 2], [1 3])
```

```
X =  1     2     3     4
     5     6     7     8
     9    10    11    12
```

```
C = [          1]    [1x3 double]
     [2x1 double]    [2x3 double]
```

Structure Array

- Each structure contains several elements
- Each element has several fields, such as: name, student id, and scores
- These fields may be in different data types

Example of Structure Array

- We create and dump the first element in a structure array

```
>> student.name = 'Bear Hsu';  
student.id = '12345678';  
student.scores = [10, 20, 30];  
>> student  
student =  
    name: 'Bear Hsu'  
    id: '12345678'  
    scores: [10 20 30]
```

Example of Structure Array (cont.)

- Add one more element to the structure array

```
>> student(2).name = 'Scoly Shih';  
student(2).id = '12345679';  
student(2).scores = [25, 36, 92];  
>> student  
student =  
1x2 struct array with fields:  
    name  
    id  
    scores
```

Print the Content of Structure Array

```
>> student(2)
ans =
    name: 'Scoly Shih'
    id: '12345679'
    scores: [25 36 92]
```

```
>> student(2).scores
ans =
    25    36    92
```

Create Structure Array using Struct

- `structureArray = struct(field1, value1, field2, value2,....)`
- If `value1, value2,`, are cell arrays, matlab will create multiple elements in structure array

```
student = struct('name', {'Bear', 'Scoly'},  
'scores', {[50 60], [60 70]});
```

```
student(1)
```

```
student(2)
```

Create Structure Array using Struct (cont.)

- If value1, value2,, are scalar, matlab will expand it and assign to all elements ← like default values

```
student = struct('name', {'Bear', 'Scoly'},  
'scores', [0, 0]);
```

```
student(1)
```

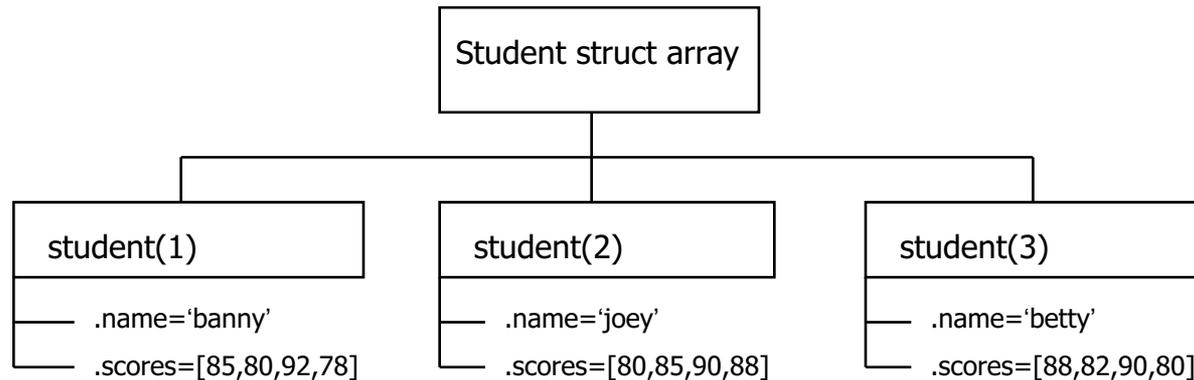
```
student(2)
```

Nested Struct Arrays

```
student = struct('name', {'Bear', 'Scoly'},  
'scores', {[50 60], [60 70]});  
student(2).course(1).title = 'Web  
Programming';  
student(2).course(1).credits = 2;  
student(2).course(2).title = 'Numerical  
Method';  
student(2).course(2).credits = 3;  
student(2).course
```

Another Struct Example

```
student(1) = struct('name', 'Banny', 'scores', [85,80,92,78]);  
student(2) = struct('name', 'Joey', 'scores', [80,85,90,88]);  
student(3) = struct('name', 'Betty', 'scores', [88,82,90,80]);
```



Use Cell Array to Access Elements

```
>> values = struct2cell(student)
values(:,:,1) =
    'Banny'
    [1x4 double]
values(:,:,2) =
    'Joey'
    [1x4 double]
values(:,:,3) =
    'Betty'
    [1x4 double]
>> size(values)
ans = 2     1     3
```

- If the input struct array is $m \times n$ with p fields, the cell array has dimension $p \times m \times n$

Editing Struct Array

```
>> student(2)
```

```
ans =
```

```
    name: 'Joey'
```

```
  scores: [80 85 90 88]
```

```
>> student(2).name = 'Bear';
```

```
>> student(2)
```

```
ans =
```

```
    name: 'Bear'
```

```
  scores: [80 85 90 88]
```

Extract Scores from Struct Array

- `A = cat(dim, structureField)` ← turn numbers into numerical array
 - `dim=2` for row arrangement
 - `dim=1` for column arrangement

```
>> cat (1, student.scores)
```

```
ans =
```

```
85      80      92      78
```

```
80      85      90      88
```

```
88      82      90      80
```

```
>> cat (2, student.scores)
```

```
ans =
```

```
85      80      92      78      80      85      90      88      88
```

```
82      90      80
```

Calculating Average

- Average score per exam
- Average score per student

```
>> mean(cat (1, student.scores))
```

```
ans =
```

```
84.3333 82.3333 90.6667 82.0000
```

```
>> mean(cat (1, student.scores) `)
```

```
ans =
```

```
83.7500 85.7500 85.0000
```

Flatten a Field

```
>> allScores = [student.scores]
```

```
allScores =
```

```
      85      80      92      78      80      85      90      88
88      82      90      80
```

```
>> allNames = {student.name}
```

```
allNames =
```

```
      'Banny'      'Bear'      'Betty'
```

```
>> allName = [student.name]
```

```
allName =
```

```
BannyBearBetty
```

Iterating Through Struct Array

```
>> for i = 1:length(student)
    fprintf ('student %g: %s\n', i,
student(i).name);
end

student 1: Banny
student 2: Bear
student 3: Betty
```

Get and Change Values of a Field

- `fieldValues = getfield (structureArray, {arrayIndex}, field, {fieldIndex})`
- `newStructure = setfield (structureArray, {arrayIndex}, field, {fieldIndex})`
- The following two statements are the same
 - `>> score3 = getfield(student, {2}, 'scores', {1})`
 - `>> score3 = student(2).scores(1);`
- The following two are the same
 - `>> student = setfield(student, {2}, 'scores', {1}, 75);`
 - `>> student(2).scores(1)=75;`

Get All Field Names

- `fieldnames(.)` returns a cell array of strings

```
>> student = struct('name', 'Roland', 'scores', [80,  
90]);
```

```
>> allFields = fieldnames(student)
```

```
allFields =  
    'name'  
    'scores'
```

Add Fields

- Matlab automatically fills in empty fields

```
>> student(2).age = 20;
```

```
>> student(1)
```

```
ans =
```

```
    name: 'Roland'  
   scores: [80 90]  
    age: []
```

```
>> student(2)
```

```
ans =
```

```
    name: []  
   scores: []  
    age: 20
```

Remove Fields

- `New_struct = rmfield(struct, field)`

```
>> student2 = rmfield(student, 'scores');
```

```
>> fieldnames(student)
```

```
ans =
```

```
    'name'
```

```
    'scores'
```

```
    'age'
```

```
>> fieldnames(student2)
```

```
ans =
```

```
    'name'
```

```
    'age'
```

Test Variables

- `isstruct(.)` tests if a variable is a struct
- `isfield(.)` tests if a struct array contains a field

```
s = struct('name', {'Tim', 'Ann'}, 'scores',  
{[1 3 5 ], [2 4 6]});  
disp(isstruct(s));  
fprintf('isfield(s, 'height') = %d\n',  
isfield(s, 'height'));
```

Convert Cell Array into Struct

- `s = cell2struct(values, fields, dim)` ← `dim` indicates which dimension should the `fieldname` be mapped to

```
fields = {'name', 'age'};  
values = {'Tim', 9; 'Annie', 6};  
s = cell2struct(values, fields, 2);  
s(1)  
s(2)
```

Convert Cell Array into Struct (cont.)

```
>> s = cell2struct(values, fields, 1);
```

```
s(1)
```

```
s(2)
```

```
ans =
```

```
    name: 'Tim'
```

```
    age: 'Annie'
```

```
ans =
```

```
    name: 9
```

```
    age: 6
```

Example: dir(.)

```
>> dirinfo = dir(matlabroot)
dirinfo =
28x1 struct array with fields:
    name
    date
    bytes
    isdir
    datenum
```

```
>> dirinfo(1).name
ans =
.
```

```
>> dirinfo(1).isdir
ans =
    1
```

Matlab #4 Homework (M4)

1. (3%) Write a single-player 3D 4x4x4 tic-tac-toe game.
 - (1%) Please design your own user-interface. (Copying code from your classmates will lead to 0 point)
 - (1%) Implement the game logic in your program, for example, each player (AI and human) takes turn to place the next marker.
 - (1%) You need to design and implement an AI to play with the user. You need to write a short report on your AI design.